Statement: The beam in Figure P6-11*b* is subjected to a sinusoidal force-time function with $F_{max} = F$ and $F_{min} = F/2$, where *F* and the beam's other data are given in row *a* of Table P6-5. Find the stress state in the beam due to this loading and choose a material specification that will give a safety factor of 1.5 for N = 5E8 cycles.



Solution: See Figure 6-24 and Mathcad file P0624a.

Free Body Diagram for Problem 6-24

1. The minimum, maximum, alternating, and mean components of the loads are:

$$F_{max} \coloneqq F \qquad F_{max} = 500N \qquad F_{min} \coloneqq \frac{F}{2} \qquad F_{min} = 250N$$

$$F_a \coloneqq \frac{F_{max} - F_{min}}{2} \qquad F_a = 125N \qquad F_m \coloneqq \frac{F_{max} + F_{min}}{2} \qquad F_m = 375N$$

2. Calculate the alternating and mean components of the maximum bending moment on the beam using the equation in Figure D-1(a) in Appendix D.

$$M_a := F_a \cdot L$$

 $M_m := F_m \cdot L$
 $M_m = 375 N \cdot m$

3. Calculate the alternating and mean components of the maximum bending stress in the beam using equation (4.11b). These are principal stresses and also von Mises stresses.

$$\sigma'_{a} := \frac{M_{a} \cdot c}{I} \qquad \qquad \sigma'_{a} = 87.719 MPa$$

$$\sigma'_{m} := \frac{M_{m} \cdot c}{I} \qquad \qquad \sigma'_{m} = 263.158 MPa$$

4. Calculate the beam cross-section dimensions from I and c.

Beam depth
$$h := 2 \cdot c$$
 $h = 40 \, mm$
Beam width $w := \frac{12 \cdot I}{h^3}$ $w = 5.344 \, mm$

5. Calculate the endurance limit modification factors for a nonrotating rectangular beam.

$$N_d = \frac{S_e(S_{ut}) \cdot S_{ut}}{\sigma'_a \cdot S_{ut} + \sigma'_m \cdot S_e(S_{ut})}$$

8. Solve the equations in steps 6 and 7 simultaneously for the desired S_{ut} .

$$S_{ut} := \frac{N_d \cdot \left(2 \cdot \sigma'_a + C_{load} \cdot C_{size} \cdot C_{surf} \cdot C_{temp} \cdot C_{reliab} \cdot \sigma'_m\right)}{C_{load} \cdot C_{size} \cdot C_{surf} \cdot C_{temp} \cdot C_{reliab}}$$

 $S_{ut} = 676 MPa$

9. Choose AISI 1060 hot-rolled steel (see Appendix C, Table C-9).